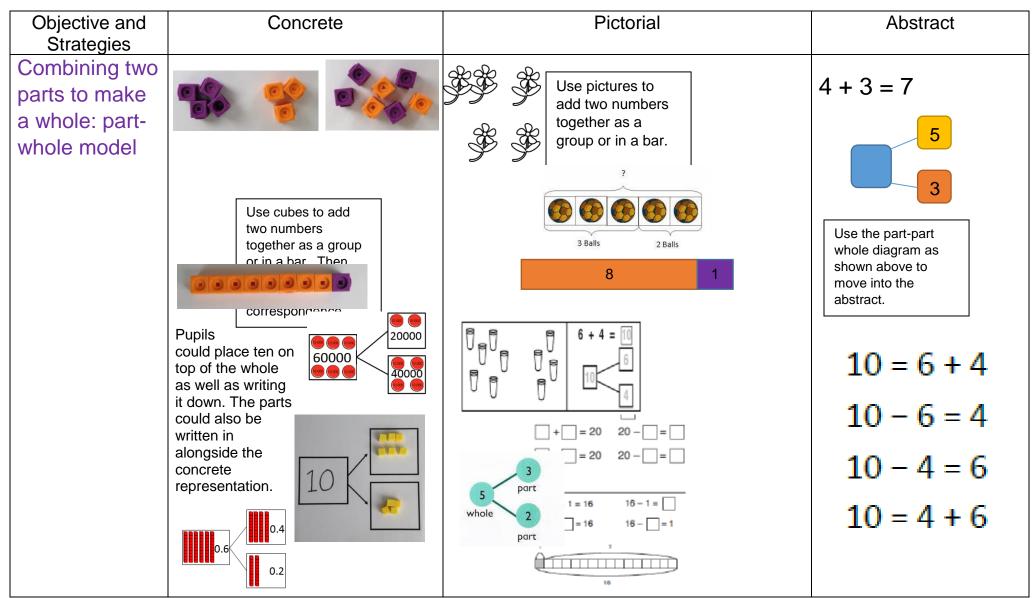
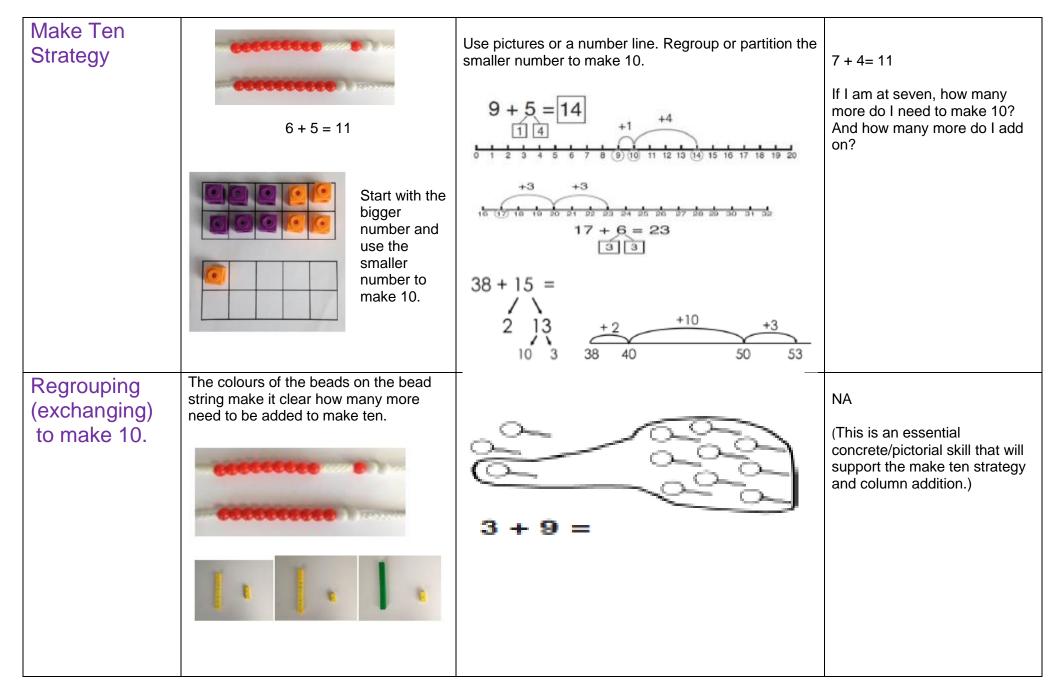


# **Addition**

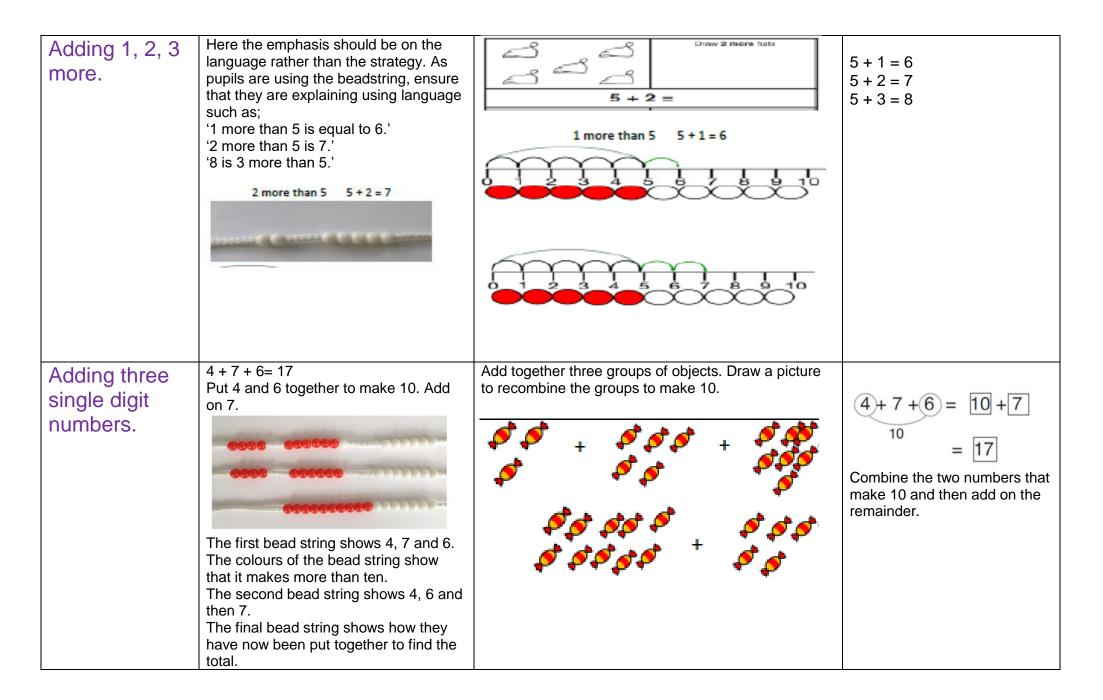
## Maths Calculation Policy



Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17 $10 + 11 + 12 + 13 + 14 + 15 + 16 + 17 + 18 + 19 + 20$ Start at the larger number on the number line and count on in ones or in one jump to find the answer. $314 + 1 = 9$	5 + 12 = 17 Place the larger number in your head and count on the smaller number to find your answer.



Adding multiples of 10	Using the vocabulary of 1 ten, 2 tens, 3 tens etc. alongside 10, 20, 30 is important, as pupils need to understand that it is a <b>ten</b> and not a one that is being added. 50 = 30 + 20		+ 5 tens = 30 + 50 =		50 + 20 = 70 Children could count up in tens 50, 60, 70 or may recognise their number bonds $5 + 2 = 7$ so $50 + 20 = 70$ .

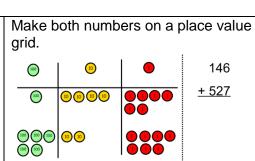


Partitioning one number, then adding tens and ones.	Pupils can choose themselves which of the numbers they wish to partition. Pupils will begin to see when this method is more efficient than adding tens and taking away the extra ones, as shown.	+10 22 32 22 + 17 = 39	+7 39	22 + 17 = 39 Counting up in head: 22, 32, 39.
Partitioning one number then counting 'on'.	Partition with cubes, dienes, bead string, counters, place value counters.	Pupils should be exposed to situation build an understanding of the fact the order in which the parts are added not change the result. +10 000 + 54 623 64 623 +77 + 300 +12 000 54 623 54 700 55 000	nat changing the	Partitioning a number in their heads e,g, 1359 1 thousand 3 hundreds five tens nine ones
Using known facts (I know, so)		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	3 + 4 = 7 leads to 30 + 40 = 70 leads to 300 + 400 = 700	$5 \times 4 = 20$ So $50 \times 4 = 200$ So $50 \times 40 = 2000$ Etc. Reasoning chains can be of great use to encourage children to use their known facts.

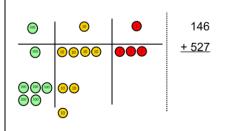
			Using near doubles e.g. 2.4 + 2.5 = double 2.4 + 0.1
Column	24 + 15=	After practically using the base 10 blocks and place	
method- no	Add together the ones first then add the tens. Use the Base 10 blocks first before	value counters, children can draw the counters to help them to solve additions.	
regrouping	moving onto place value counters.	то	232
(exchanging)	tens ones ters ones		+ 2 2 6
			4 5 8
		$ \begin{array}{c c} \hline \hline rers & \hline Ones \\ \hline \hline \hline \hline \hline \hline \\ \hline \hline \hline \\ \hline \hline \hline \\ \hline \hline \hline \hline \hline \\ \hline \hline \hline \hline \hline \hline \hline \\ \hline \hline$	4 2 + 2 6 6 8

+

## Column methodregrouping (exchanging)



Add up the units and exchange 10 ones for one 10.

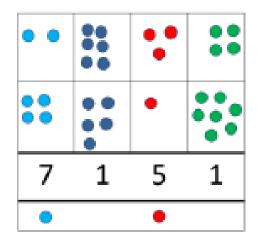


Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

As children move on to decimals, money and decimal place value counters can be used to support learning.



Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.



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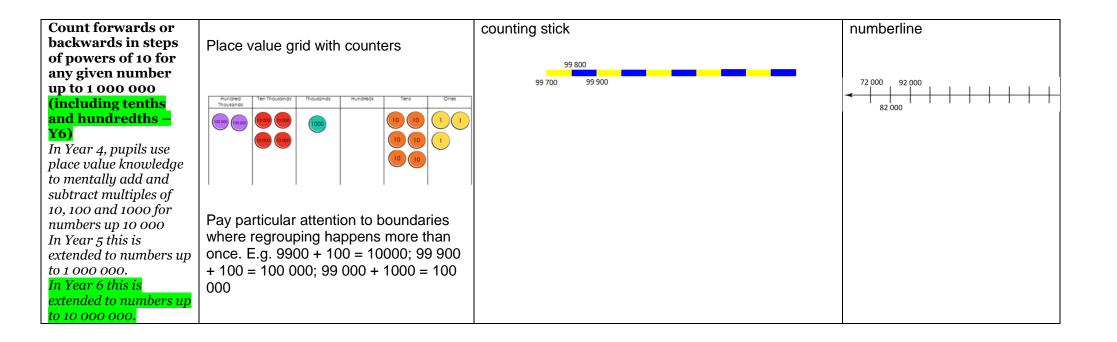
 i
 i

Start by partitioning the numbers before moving on to clearly show the regrouping below the addition.

	4	5	3	
+	2	2	7	
		1		
	6	8	0	

As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.

Use a line in between the final addend and the answer for exhanging.

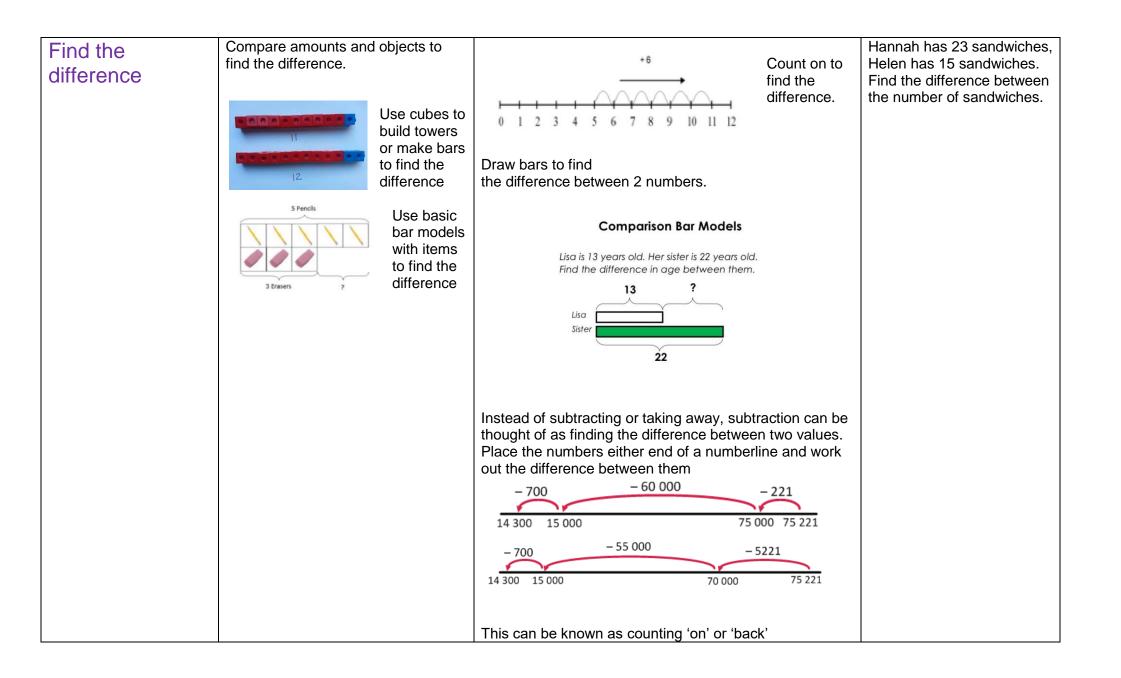




## **Subtraction**

Objective and Strategies	Concrete	Pictorial	Abstract
Taking away         Ones         When this is first         introduced, the concrete         representation should be         based upon the diagram.         Real objects should be         placed on top of the         images as one-to-one         correspondence,         progressing to         representing the group         of ten with a tens rod         and ones with ones         cubes.	Use physical objects, counters, cubes etc to show how objects can be taken away. 6-2=4	Cross out drawn objects to show what has been taken away. $28 - 4 =$ $\begin{array}{c} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	18 -3= 15 8 - 2 = 6

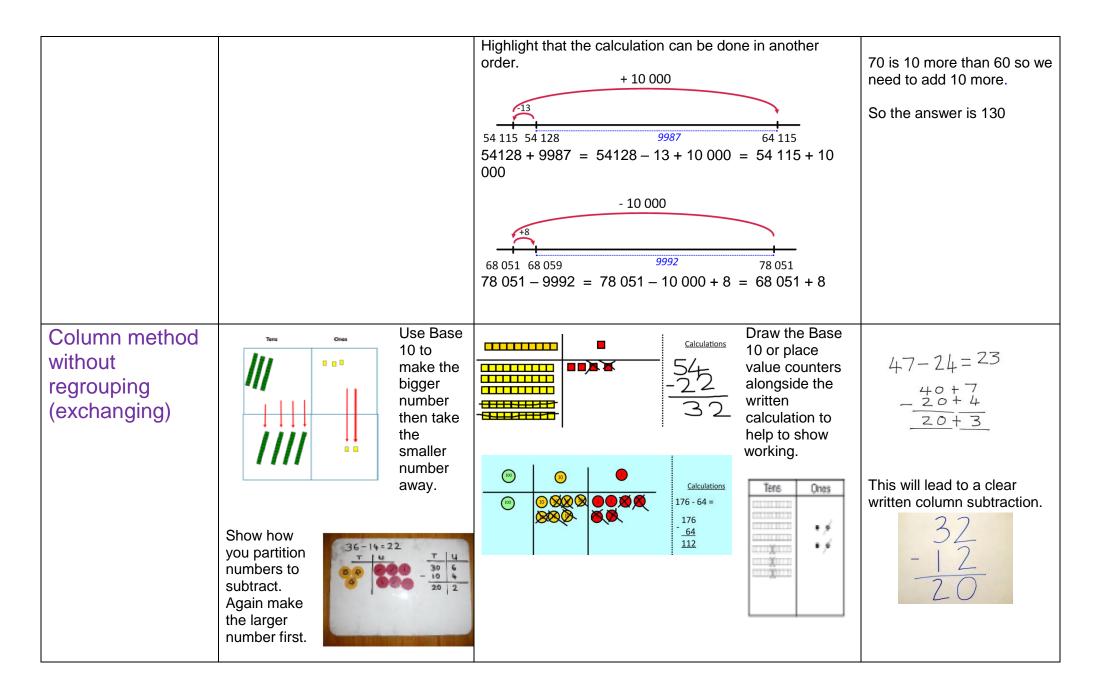
Part-part-whole	Pupils could place ten on top of the whole as well as writing it down. The parts could also be written in		10 = 6 + 4
			10 - 6 = 4 10 - 4 = 6
	10		10 = 4 + 6
	alongside the concrete representation.		
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.
	<ul><li>13 – 4</li><li>Use counters and move them away from the group as you take them away counting backwards as you go.</li></ul>	-10 -10 -10 -10 -10 -10 -10 -10 -10 -10	
		This can progress all the way to counting back using two 2 digit numbers.	

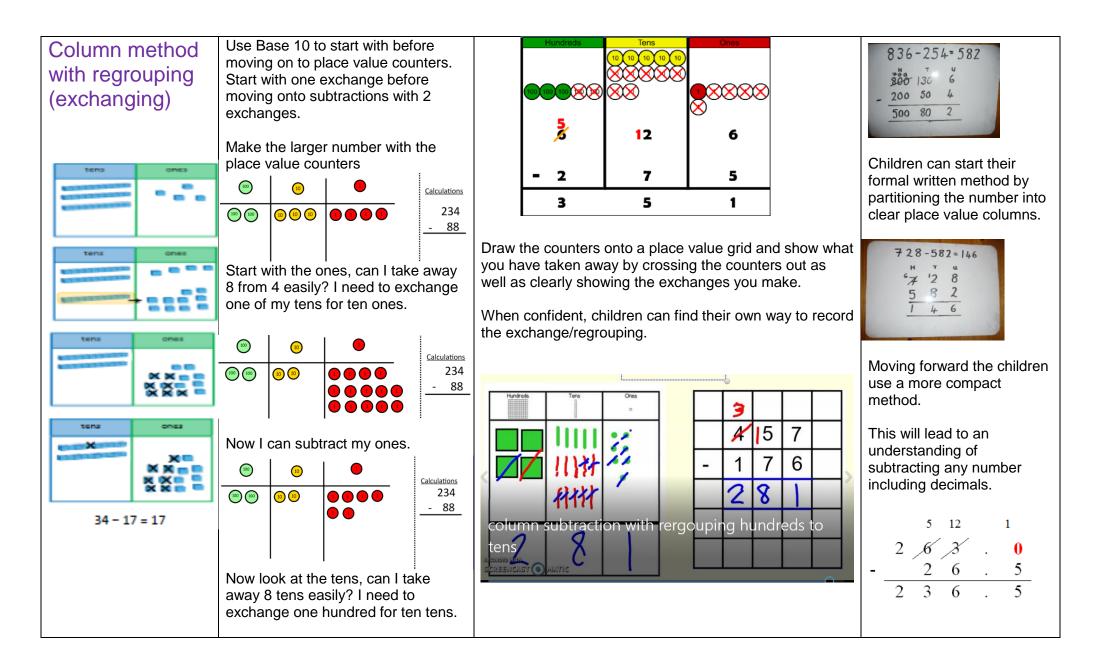


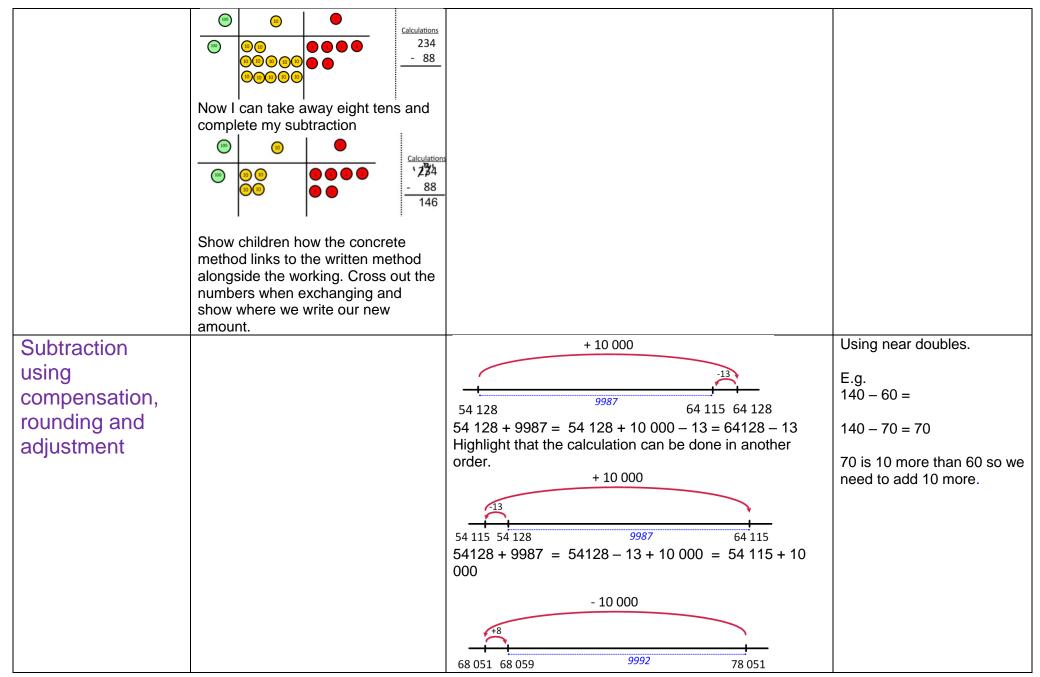
Part Part Whole Model	Link to addition- use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? 10 - 6 =	Use a pictorial representation of objects to show the part- part-whole model.	5 10 Move to using numbers within the part whole model.
Make 10	14 – 9 = Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.	13 - 7 = 6 3 4 5 1 2 5 4 5 6 7 5 5 10 11 12 (3 14 15 16 17 16 19 20) Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 – 8= How many do we take off to reach the next 10? How many do we have left to take off?
Subtracting tens and adding extra ones. Pupils must be taught to round the number that is being subtracted.	53 - 17 = 36	-20 33 + 3 56 53	53 - 17 = 36 Round 17 to 20. 53 - 20 = 33 20 - 17 = 3 (number bonds)

Pupils will develop a sense of efficiency with this method, beginning to identify when this method is more efficient than subtracting tens and then ones.		53 - 17 = 36	33 + 3 = 36 (we add because we took an extra 3 away when we subtracted 20 instead of 17).
Subtracting Multiples of Ten	Using the vocabulary of 1 ten, 2 tens, 3 tens etc. alongside 10, 20, 30 is important as pupils need to understand that it is a <b>ten</b> not a one that is being taken away. 40 = 60 - 20 38 - 10 = 28 40 = 60 - 20 38 - 10 = 28	$5 \text{ tens} - 2 \text{ tens} = \ \text{tens}$	32 – 10 = 22 Look at the number of tens in the largest number. Count back in tens to subtract the smaller number. 30, 20. Add on the number of ones that we originally had. = 22

Counting back in multiples of ten and one hundred.	Removing one group of 10 each time.	-10 -10 75 85 95 -100 -100 750 850 950	Counting back in 10s or 100s from any starting point. 53, 43, 33 540, 440, 340
Take away		Parts are place value amounts (canonical partitioning) -300 - 4000 - 10000 To 421 Pupils should understand that the parts can be subtracted in any order. Parts are not place value amounts (non canonical partitioning) Make ten, make hundred, make thousand, make one -9000 - 5000 - 221 6092161000 - 221 -79 - 14000 - 221 -79 - 14000 - 221 -79 - 14000 - 221	
Addition using compensation, rounding and adjustment		$\begin{array}{r} +10\ 000 \\ \hline \\ 54\ 128 \\ 54\ 128 + 9987 = 54\ 128 + 10\ 000 - 13 = 64128 - 13 \end{array}$	Using near doubles. E.g. 70 + 60 = 60 + 60 - 120



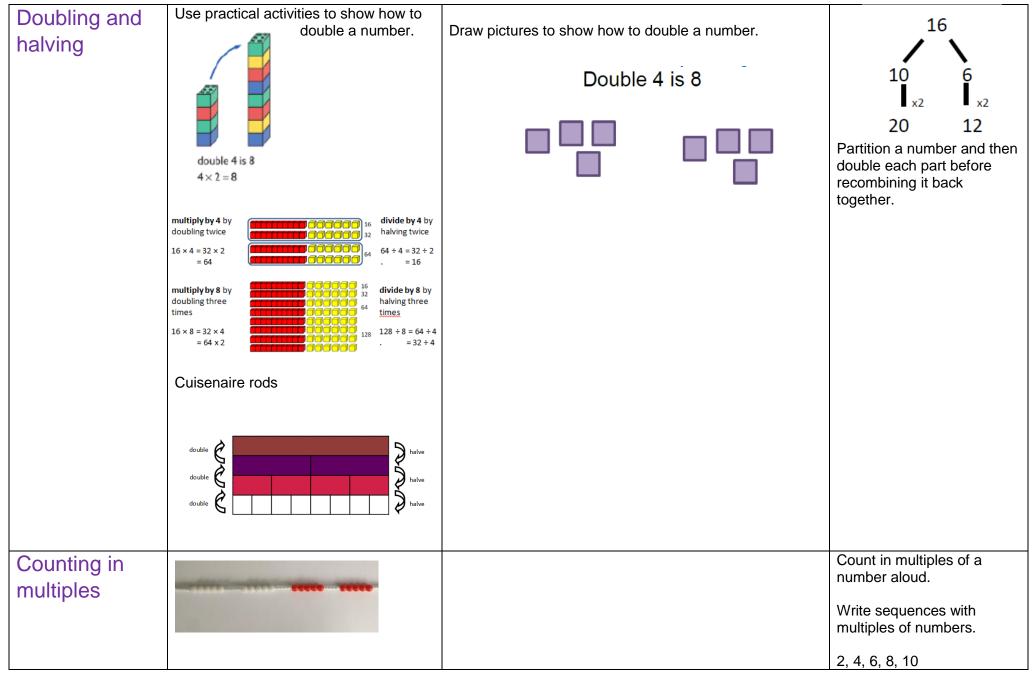




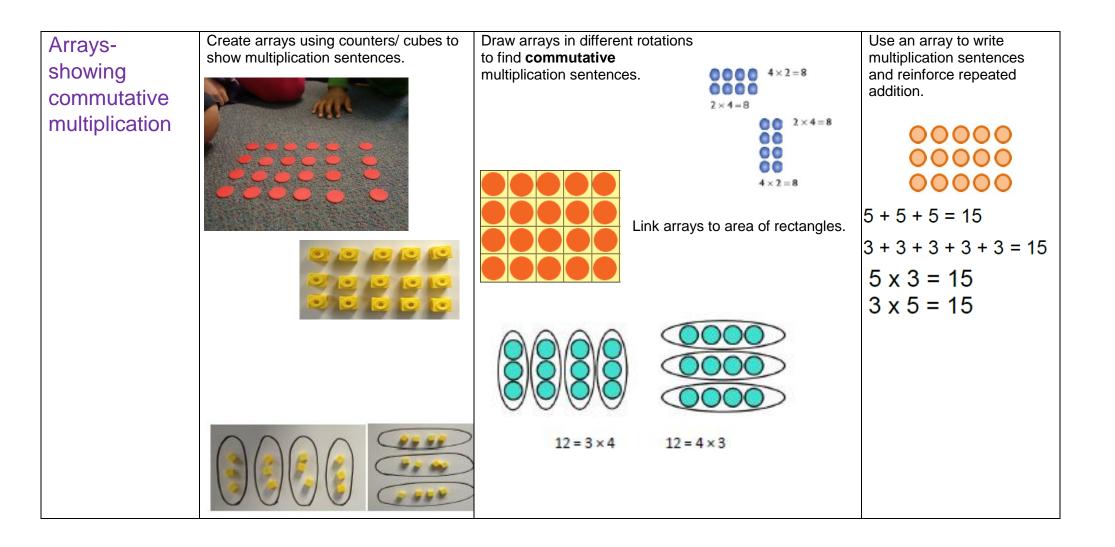
		78 051 - 9992 = 78 051 - 10 000 + 8 = 68 051 + 8	
AND STELD PRIMARP. PC			
Multip	<u>olication</u>		

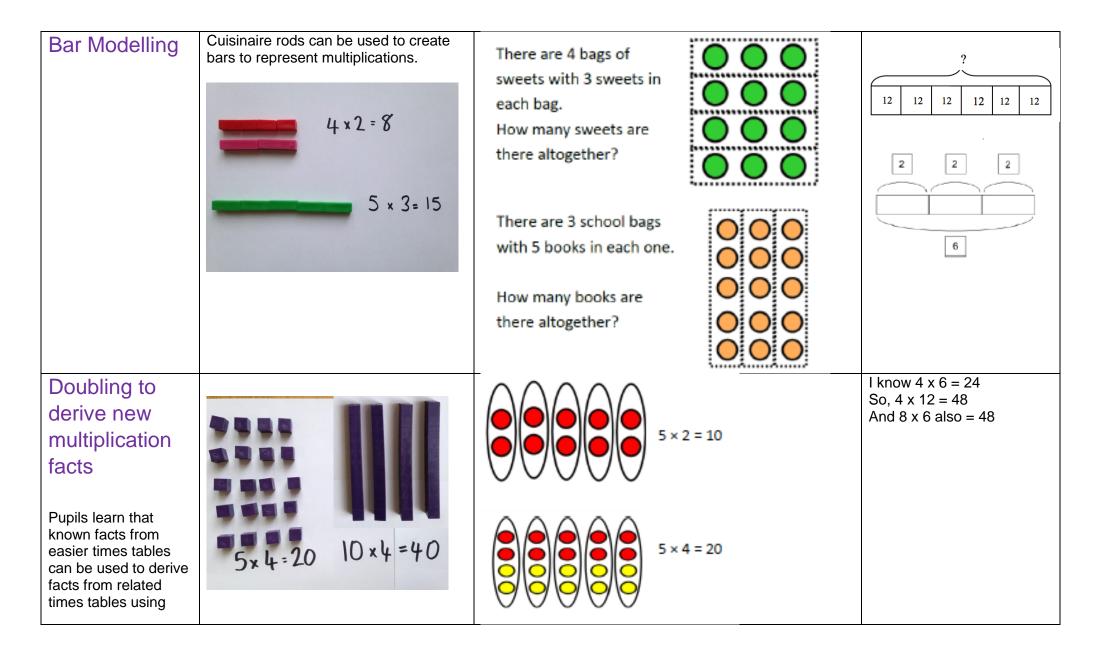
## Multiplication

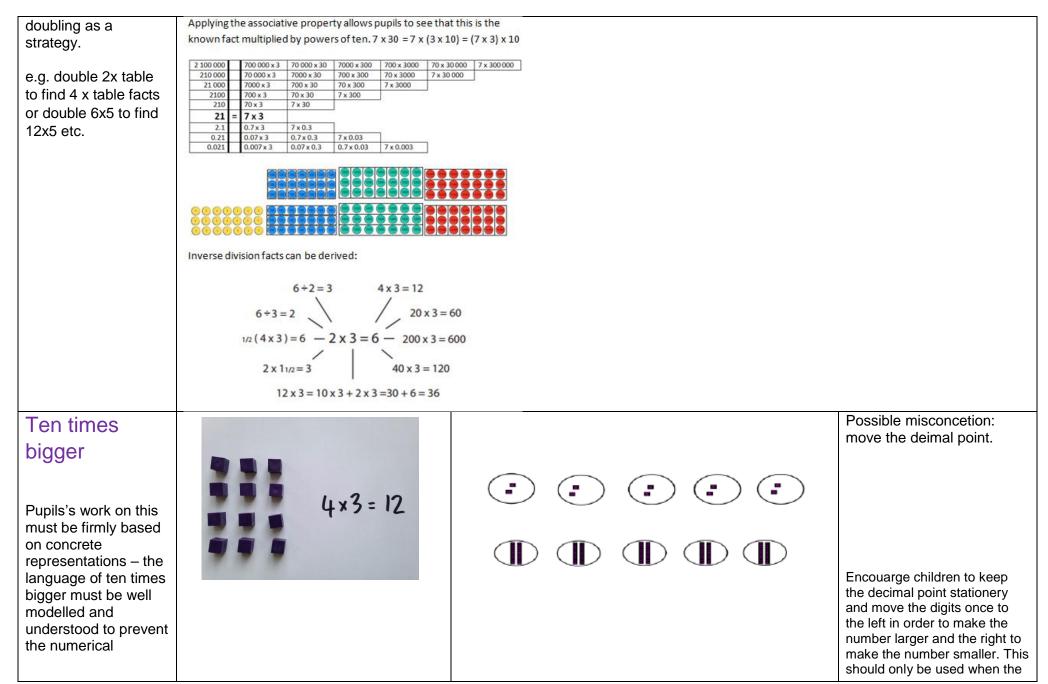
Objective and	Concrete	Pictorial	Abstract
Strategies			

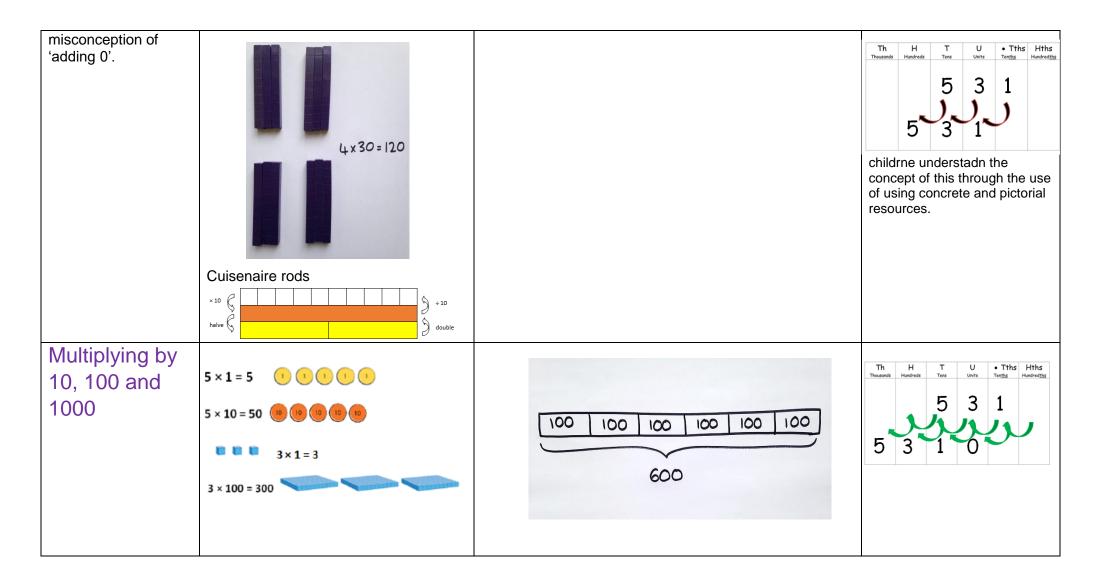


	Count in multiples supported by concrete objects in equal groups.	MA       MA <th< th=""><th>5, 10, 15, 20, 25 , 30</th></th<>	5, 10, 15, 20, 25 , 30
Repeated	$ \begin{array}{c}                                     $	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?	Write addition sentences to describe objects and pictures.
addition		$ \begin{array}{c}  \\  \\  \\  \\  \\  \\  \\  \\  \\  \\  \\  \\  \\ $	2+2+2+2=10









Distributive property	You can use dienes, counters etc. to illustrate this using arrays. Drawing out the boxes (see right) and building them up can be useful.	x 8 is 7 x 4 a 4 7	4	7 x 4: 7 x 8 5 2	1 1	2 x 8: 2 18 5 45
Multiplication of 2 digit numbers with	3 x 12 12 = 10 + 2 3 X 10 3 X 2	×	10	2	]	3 x 12 10 and 2 make 12 3 x 2 = 6
partitioning (no regrouping)		3	Ξ	:::	]	$3 \times 10 = 30$ 30 + 6 = 36
		×	10	2		
	Now add the total number of tens and ones.	3	30	6		
			3 x 12 =	36		

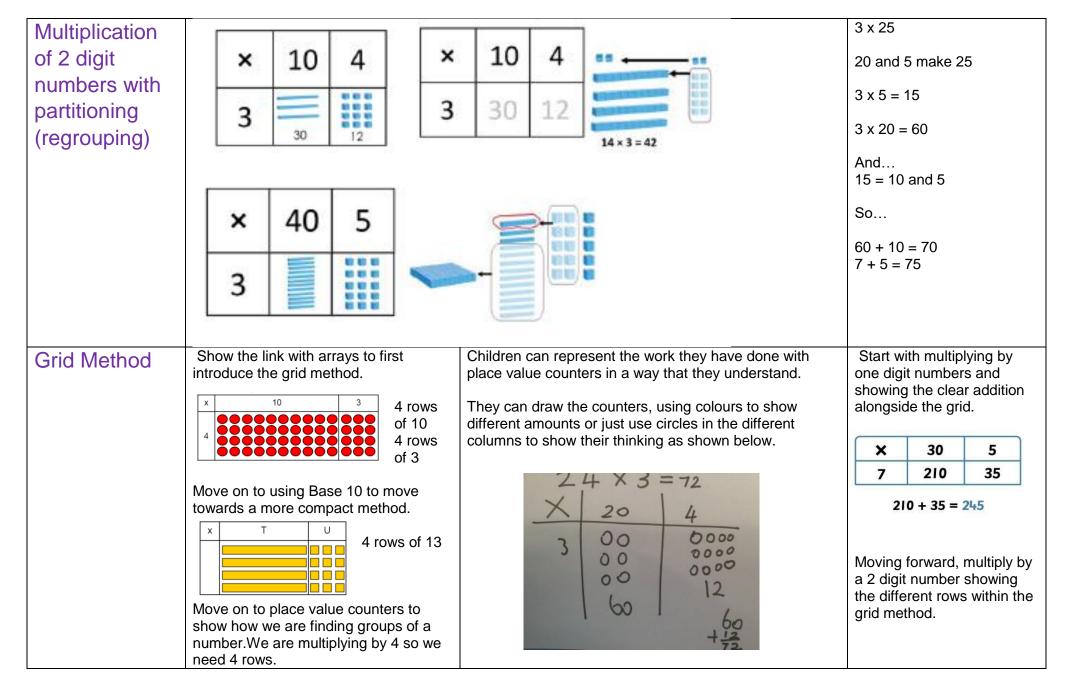
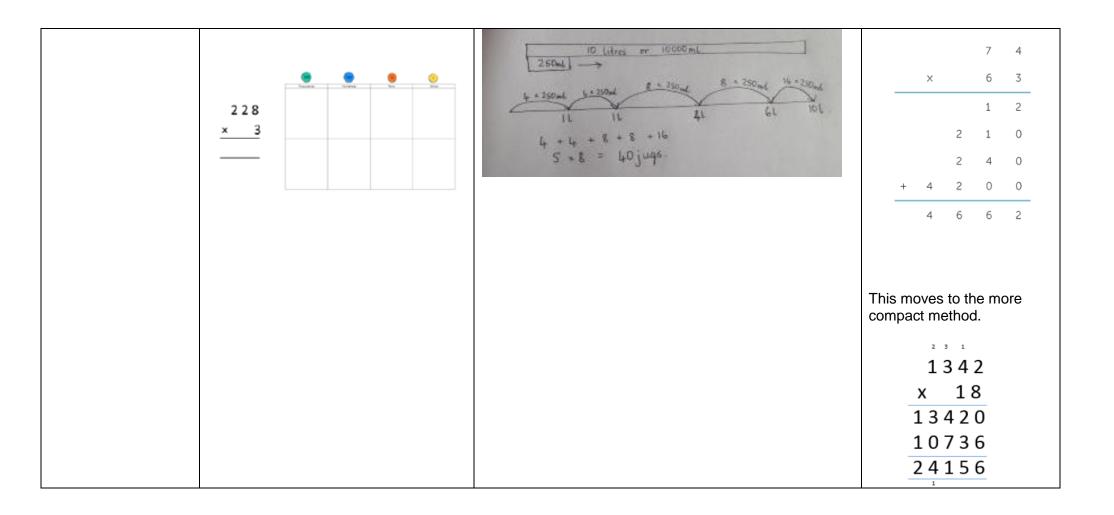


	Image: Second		10		10 100		8 80
	Fill each row with 126.		3		30		24
	Calculations		Х	1000	300	40	2
	4 x 126		10 8	10000 8000	3000 2400	400 320	20 16
	Add up each column, starting with the ones making any exchanges needed.						
Short multiplication	It is important at this stage that children always multiply the ones first and note down their answer followed by the tens which they note below.	Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.	multi childı	ren ab	on, rei out lin	ing u	ng the p their umns.
	6° 3 6° 6° 6° 6° 6° 6° 6° 6° 6° 6° 6° 6° 6°	$51 59 59 59 59 59 59 59$ $8 \times 59$ $8 \times 60 - 8$ $8 \times 60 - 8$ $8 \times 60 = 480$ $480 - 8 = 472$	out w	elps, c hat th to thei $x \frac{24}{8}$ 120 40 <u>600</u> 768	ey are ir ansv (4 ) (20	e solv ver.	-



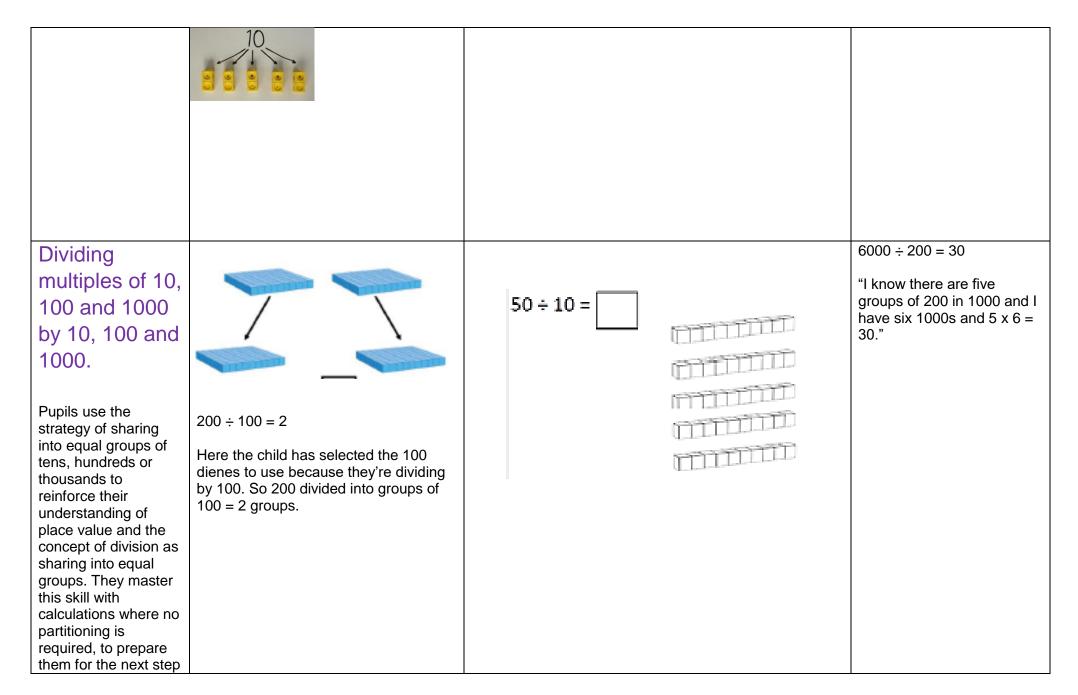
National Curriculum appendix:

### Long multiplication

$24 \times 16$ becomes	124 × 26 becomes	124 × 26 becomes
2	1 2	1 2
Note <sup>2</sup> Use a line in	between the final factor	124
and the answer fo	r exhanging, rather <sup>6</sup> than in	× 26
	left. 2 4 8 0	7 4 4
144	744	2480
3 8 4	3 2 2 4	3 2 2 4
	1 1	1 1
Answer: 384	Answer: 3224	Answer: 3224



Objective and Strategies	Concrete	Pictorial	Abstract
Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. Children use pictures or shapes to share quantities. 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 +	Share 9 buns between three people. $9 \div 3 = 3$
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 3 3	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	
		20 ? 20 ÷ 5 = ? 5 x ? = 20	



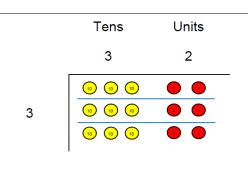
Division within arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Image: Constraint of the sector of the se	Find the inverse of multiplication and division sentences by creating four linking number sentences. $7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$
Division with a remainder	14 ÷ 3 = Divide objects between groups and see how much is left over	Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder. 0 4 8 12 13 Draw dots and group them to divide an amount and clearly show a remainder. () () () () () () () () () () () () () (	Complete written divisions and show the remainder using r. $29 \div 8 = 3$ REMAINDER 5 $\uparrow \uparrow \uparrow \uparrow \uparrow \uparrow$ dividend divisor quotient remainder



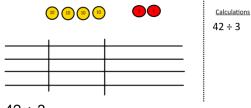
The difficulty with the short division algorithm comes with the confusion that can be caused by what you "think in your head" The thought process of the traditional algorithm is as follows: How many 4s in 8? 2 How many 4s in 5? 1 with 1 remaining so regroup. How many 4s in 12? 3 How many 4s in 8? 2 Warning: If you simply knowledge to each step,

Warning: If you simply apply place value knowledge to each step, the thinking goes wrong if you have to regroup. How many 4s in 500? 100 with 1 remaining (illogical) The answer would be 125 Sharing the dividend builds conceptual understanding however doesn't scaffold the "thinking" of the algorithm.

Using place value counters and finding groups of the divisor for each power of ten will build conceptual understanding of the compact short division algorithm.



Use place value counters to divide using the bus stop method alongside



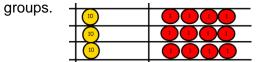
#### 42 ÷ 3=

Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.



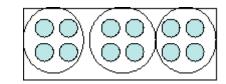


We exchange this ten for ten ones and then share the ones equally among the

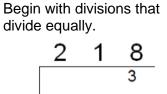


We look how much there is in 1 group; the answer is 14.

Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.

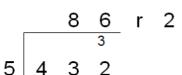


Encourage them to move towards counting in multiples to divide more efficiently.

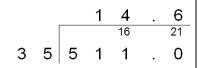




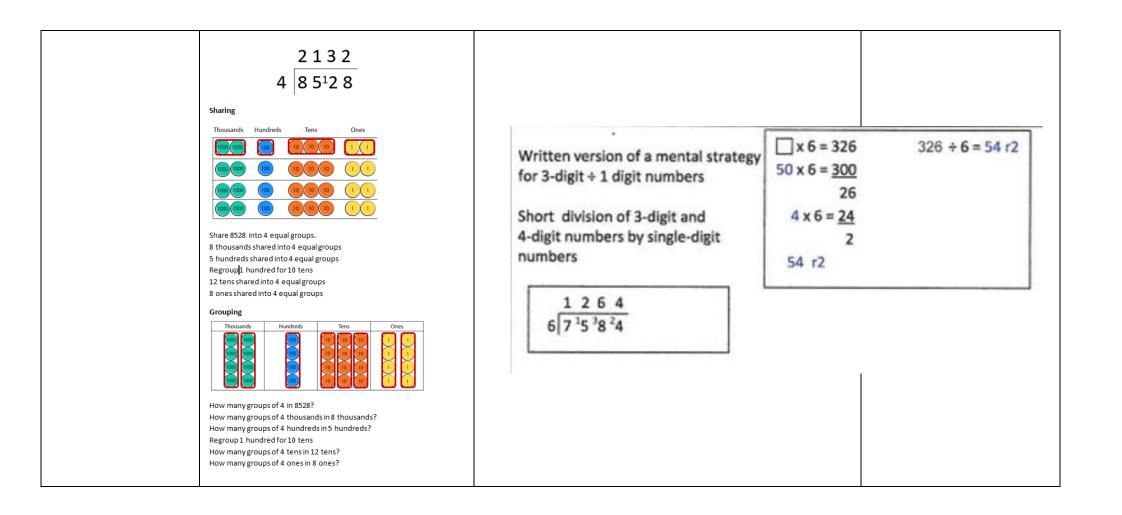
Move onto divisions with a remainder.



5 4 3 2 Finally move into decimal places to divide the total accurately.



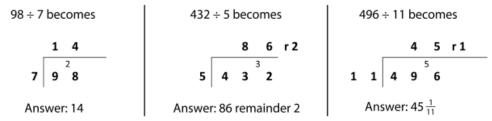
See below for written strategies:



Long Division	The short division method can be applied for 11 and 12 using times tables knowledge. Factors shoul dbe used to break down the calculation and apply the short division method. If the divisor is a print number see opposite.	$ \begin{array}{c c} 2 1 2 \\ 13 \overline{)2756} \\ \underline{26} \\ 15 \\ \underline{13} \\ 26 \\ \underline{26} \\ 0 \end{array} $	212 132756 2600 156 <u>130</u> 26 <u>26</u> 0
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National Curriculum appendix:

#### Short division



#### Long division

432 ÷ 15 becomes	432 ÷ 15 becomes	432 ÷ 15 becomes
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$